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IMPROVING ADVANCE TRANSFER TECHNIQUE: MANOEUVRING ANALYSIS USING A BULK CARRIER SHIP WHILE IN BALLAST CONDITION

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ABSTRACT

A wheel over point is specified on the charted courses in a voyage plan to indicate the point at which the ship must change direction. A late course alteration would result in an overrun of the intended course line, which can be observe by the expansion of cross-track distance. The wheel over point may be computed using the advanced transfer technique. Through a practical assessment of ATT, the research was able to identify a few gaps. The data included in the manoeuvring characteristics, particularly advance and transfer, were then utilised to develop an IATF capable of bridging the gaps. Following that, a manoeuvring study was conducted and data, including the cross-track distance, were acquired. Compliance with cross track limits and percentage change were utilised to validate the simulation analysis findings. The results demonstrated that the enhanced mathematical model was capable of providing better track keeping and was thus suited for use onboard a cargo ship.

ARTICLE INFO

Keywords: Wheel Over Point, Alteration Course, Advance Transfer Technique, Passage Planning, Cross-Track Distance

1.0 INTRODUCTION

A ship navigates by following one course line to another course line connected by waypoints (WPT) to complete a voyage as according to the agreed passage plan prepared by the ship's wheelhouse team (ICS, 2016; Lušić et al., 2014). Failure to do so can lead to an accident (Marine Insight, 2020). Safety of ship's operations relies upon seafarers' communication, teamwork, leadership, situational awareness, result focus, decision making and desire to learn and to develop (Kamis et al., 2020). Looking at a report by Gale & Patraiko (2007), 17% of grounding incidents were caused by poor passage planning. Passage planning is a method for creating a detailed overview of the vessel's voyage from the port of departure to the port of arrival (IMO, 1999).



Figure 1. Various connected charted course in a voyage plan on a nautical chart Charting courses line is one of the activities during the planning phases (IMO, 1999; Swift, 2018). As shown in Figure 1, the charted course is the course line drawn on the navigational chart connected by waypoints (ICS, 2016; IMO, 1999). Waypoint (WPT) is the point where two different course lines are connected (ICS, 2016; Swift, 2018). After completion of the planning phase, the passage plan will be executed followed by monitoring of the plan which includes ships operational status such as weather conditions, fuel consumption, collision regulations and maintaining its planned track (Swift, 2018; Zekić et al., 2015). When changing a course, the alteration needs to be carried out at an ample distance to avoid the ship from overshooting from the planned track (Vujičić et al., 2018). For this reason, a wheel over point (WOP) needs to be accurately calculated and marked on the charted course as an indication of the alteration point (Bielek, 2020; Georgiana & Stefan, 2010).

2.0 PROBLEM STATEMENT AND THE AIMS OF THE STUDY

Onboard ship, the advance transfer technique (ATT) with manual calculation on a navigational chart is the most common method of determining WOP (Anwar, 2015). Manual calculation has a few disadvantages, such as being time consuming and only being applicable to paper charts (Anwar, 2015). Apart from that, two issues with the ATT were discovered during the practical exercise using a navigation chart.

- 1. The formula given by the technique is ineffective for changes of course of less than 20° (see section 4.1.1).
- 2. The final ship's heading differs from the charted direction, resulting in second overshooting (see Figure 7).

Mathematical modelling offers better results in deciding WOP as paper charts are gradually replaced electronic charts that have been introduced in maritime navigation. The aim of this study was to create a better mathematical model that used advance transfer information from a ship's manoeuvring characteristics as variables in deciding WOP (Jeong et al., 2019; Statheros et al., 2008).



3.0 METHODOLOGY



For this purpose, the study began with a simulation exercise to determine WOP using the ATT for the purpose of understanding its shortcomings. As a result, an improved model namely Improved Advance Transfer Formula (IATF) was developed. A new introduced system should be compared with the existing system to ensure the effectiveness and improvements (Voit, 2020). For this reason, a ship simulator was used to test both ATT and IATF.

The Wartsila ship simulator was used to collect data during the full-scale simulation. A series of courses for each 10° alteration were first developed using an ECDIS simulator. ATT and IATF were evaluated through the manoeuvre analysis, and the XTD for each course alteration was gathered before comparing them to analyse the improvement.

The manoeuvre simulation XTD data will be evaluated in two phases. In the first phase, the XTD for each alteration was compared to the XTL, using formula given by Kristić et al. (2020). The purpose of this phase was to see which approach produced better compliance with XTL. XTL is defined as the maximum perpendicular distance by which a ship can safely diverge from the planned track. However, although a ship needs to comply to the XTL as expressed in general by IMO (IMO MSC, 1998, 2006, 2007), IMO did not provide the exact value of XTL. Thus, this research used the recommendation in a study conducted by Kristić et al. (2020) to decide XTL for the respective ship.

Then, the validation by percentage change was carried out in the second phase to show the improvement trend over existing method. The expression "percentage change" refers to the amount of a variation over a specified period (Bansilal, 2017). It is commonly utilised for a

[Open]

variety of commercial purposes, most notably to denote price changes (Bansilal, 2017; Beck, 2020). Similarly, the percentage change in this analysis was able to illustrate the propensity of IATF to minimise XTD as compared to ATT.

3.1 THE ADVANCE TRANSFER TECHNIQUE AND THE APPLICATION

ATT is a course alteration technique that used maximum rudder angle while turning. It is frequently utilised in inland water and is preferred for pilotage since the turning circle's characteristics are not affected by the vessel's speed (Kim et al., 2005). The rudder angle specified for a particular movement has an effect on the vessel's manoeuvring characteristics (Drachev, 2012; Kim et al., 2005). Upon ship delivery, a sea trial manoeuvre will be conducted, resulting in a ship-specific manoeuvring characteristic. The turning circle for each rudder angle, as well as the diameter of the turning circle based on the loaded/ballast condition and the shallow/deep water region covered will be recorded throughout the process (IMO, 2002; ITTC, 2002; Kim et al., 2005). A shallow water region is defined as one that has a water depth less than 1.5 times the ship's draft, a medium deepwater area as one that has a water depth larger than 3.0 times the ship's draft (Duarte et al., 2016; Sian et al., 2014).



Figure 3. Ship's manouvering characteristic (ITTC, 2002)

The advance transfer technique by Anwar requires two variables namely advance and transfer from the maneuvring characteristics as seen in Figure 3. Advance and transfer distances are measured from the ship's centre of gravity (CG) (ITTC, 2002) from the instant the vessel commences the turn by turning the rudder to maximum angle until the ship's heading changes by 90 degrees, where advance is measured along the X0 axis and transfer along the Y0 axis, as seen in Figure 4 (ITTC, 2002). Anwar (2015) proposed a way to use the given information to determine the WOP as explained below;



Figure 4. WOP identification using the advance transfer technique (Anwar, 2015)

With references to Figure 5, the steps of determining WOP are as follows:

- i. At point B, extend the present course line 270°T
- ii. At any point, 'X' is on this line, draw a perpendicular line 'XY' towards the alteration so that 'XY' = Transfer
- iii. At 'Y', draw a line parallel to 'BX' so that it cuts the course line 310°T. The point at which the parallel line cuts the next course line is 'D'. Now, if the line is drawn at 'D', which is parallel to 'XY', point 'C' would be obtained on the extension of the present course line.
- iv. From 'C', measure the advance backwards i.e. in the direction 090°T (reciprocal of 270°T) to obtain point 'A'. 'A' is the WOP, where 'CA' equals advance distance.



Figure 5. Marking WOP (Anwar, 2015)

Abbreviation; $d_{adv} = Advance value$ $d_{trs} = Transfer value$ $d_{CG-WPT} = Distance from ship CG to WPT$ $d_{WOP} = Distance of WOP' from WPT$ $\theta = Change of course angle$ [Open]

According to Figure 5;

$$d_{CG-WPT} = d_{adv} - d_a \tag{1}$$

To obtain d_a the following tangent rules can be used:

$$tan \theta = \frac{d_{trs}}{d_a}$$
$$d_a = \frac{d_{trs}}{tan \theta}$$

Therefore, the equation by Anwar (2015) can be re-written as below,

$$d_{CG-WPT} = d_{adv} - \frac{d_{trs}}{\tan\theta}$$
(2)

The principle of the technique worked as shown in Figure 6, however, the final ship's heading was 090°T and did not correspond to the 045°T in which the desired course should be achieved.



Figure 6. Existing advance transfer technique (ATT) principle, ship ended up on the next course at 90° from the original course (Anwar, 2015)

3.2 OPTIMISING ADVANCE AND TRANSFER USAGE

The purpose of this study was to improve the advance and transfer techniques for estimating WOP. The ATT will be improved accordingly to make sure the final ship's heading matched the planned course.



Figure 7. Concept of the study, final heading match charted course

For this reason, this research sought to adapt the approach as illustrated in Figure 7 in order to verify that the ship's final heading matched the planned next path.

3.3 CONSTRUCTING NEW MATHEMATICAL MODEL

The ATT equation (2) was utilised as the core model for constructing the IATF. Adapting the similar concept, the following figure 8 were constructed to aid the explanation on the development of IATF.

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Figure 8. Distribution details

As shown in figure 8, the d_{WOP} which is the position of WOP measured from WPT will be divided as follow.

$$d_{WOP} = d_{CG-WPT} + d_c$$

$$d_{CG-WPT} = d_a + d_b$$

$$d_{WOP} = d_a + d_b + d_c$$
(3)

da is the distance from CG to the line perpendicular to the centre of tactical diameter, and the radius of tactical diameter is equal to transfer, hence,

$$d_a = d_{adv} - d_{trs} \tag{4}$$

 d_b is the distance between R and S, WPT or R is the intersection of present course line and next course line, and both course lines are tangent to an imaginary circle. Since both of courses line are tangent to the circle, and the QS is parallel to OU, by the rule of tangent (Mathews, 1915; Srinivasan, 2002), the angle of PRQ and PUO has the same value, $\angle PRQ = \angle PUO$, hence the change of course, $\angle PRQ$, represent by θ is equal to angle PUO, $\theta = \angle PUO$

To get d_b the following tangent rules can be applied,

$$tan \ \angle ROS = d_b / d_{trs}$$
$$d_b = d_{trs} \ x \ tan \ \angle ROS \tag{5}$$

Since RP and RS is tangent to the circle, by the rule of tangent to the circle, both distances will be the same, |RP| = |RS| so, the angle of ROS and POR is same, $\angle ROS = \angle POR$. Hence, $\angle ROS$ has half of value of $\angle POS$, so,

$$\angle ROS = \angle \frac{POS}{2}$$
$$\angle ROS = \frac{\theta}{2} \tag{6}$$

With references to equation at (3), and input from (4),

$$d_b = d_{trs} x \tan \angle ROS$$

$$d_b = d_{trs} x \tan \frac{\theta}{2}$$
(7)

Considering WOP position will be monitored using GPS, which is located at the ship's wheelhouse, the real WOP indicated on the chart should incorporate the distance between the CG and the wheelhouse, specifically the position of GPS antenna, thus $d_{CG} = d_c$, applied as follow:



Figure 9. d_{CG} is the distance between the GPS antenna and the CG

therefore,

$$d_c = d_{CG} \tag{8}$$

in summary, with references to equation (3), and input from equation (4), (7) and (8),

$$d_{WOP} = d_a + d_b + d_c$$

$$d_{WOP} = d_{adv} - d_{trs} + (d_{trs} x Tan(\frac{\theta}{2})) + d_{CG}$$

$$d_{WOP} = d_{adv} - d_{trs}(1 - Tan(\frac{\theta}{2})) + d_{CG}$$
(9)

4.0 FINDINGS AND DISCUSSION

The Wartsila Ship Simulator was used to carry out manouvering analysis to see the impact on the ship's XTD when course alteration was carried out referring to the WOP calculated by ATT and IATF. A bulk carrier with a displacement of 23565 tonnes while in ballast condition was selected for the analysis. The tests were carried out in shallow and deep water for port and starboard alternation.

View	General information	
	Vessel type	Bulk carrier 1 (Dis.23565t) bl.
	Displacement	23565.0 t
T	Max speed	15.0 knt
	Dimensions	
	Length	182.9 m
Type of engine Slow Speed Diesel (1 x 8827 kW)	Breadth	22.6 m
Type of propeller FPP	Bow draft	7.5 m
Thruster bow None	Stern draft	7.6 m
Thruster stern None	Height of eye	22 m

Figure 10. Selected ship for this study

The data regarding the chosen ship were obtained from the simulator. Nine charted courses was prepared on the ECDIS simulator and WOP for each courses were identified using ATT and IATF. A helmsman was instructed to follow the course and execute the turn at marked WOP by the application of hard rudder angle. Then, the XTD of the vessel was monitored and recorded.

4.1 DATA COLLECTION

XTD for each simulation were recorded in table 2 and 3. Two phases of analysis were conducted on the data obtained from the manoeuvring simulation. The data was first analysed by comparing the XTD to XTL. The XTL for the selected ship in this study was determined as follows:

Area A1	d_{zoc}	dbreadth	d_{pos}	d _{na}	d _{so}	XTL (m)
Restricted Water	6.5	11.3	15	50	37	119.8

Table 1: XTL value (Kristić et al., 2020)

4.2 XTD RESULT

Location and ENC	Side	θ	d_{adv}	d_{trs}	d_{CG}	d_{W})P	XTD < XTL(119.8m) ?			Comparison Graph			
number	•1		(IIII)	(IIII)	(1111)	ATT	IATF	AT	Γ (m)	IAT	'F (m)			
Kemaman,		10 °	0.24	4 0.108 0.0329 -0.372 0.174 58 YES 20 YES		VTD Bacult								
Malaysia		20°	0.24	0.108	0.0329	-0.057	0.184	115	YES	25	YES		ATD Result	
ENC		30°	0.24	0.108	0.0329	0.053	0.194	119	YES	8	YES	150 ~	125	
number:	ard	40°	0.24	0.108	0.0329	0.111	0.204	125	NO	30	YES	ete 100	115110125 105	
3JS P9200	urbo	50°	0.24	0.108	0.0329	0.149	0.215	105	YES	2	YES	<u>د</u> 50	는 0 50	58 50-48 45 ATT
04°10 78'	Sta	60°	0.24	0.108	0.0329	0.178	0.227	83	YES	12	YES	EX C	20 25 30 12 19 22 ATMM	
N		70 °	0.24	0.108	0.0329	0.201	0.241	50	YES	2	YES	0		
103°35.4'E		80°	0.24	0.108	0.0329	0.221	0.256	48	YES	19	YES		Change of course (°)	
22.0.20.2		90°	0.24	0.108	0.0329	0.240	0.273	45	YES	22	YES			
23.8-29.3m —		10 °	0.23	0.102	0.0329	-0.348	0.17	84	YES	6	YES		VTD Bocult	
(ueep water)		20°	0.23	0.102	0.0329	-0.050	0.179	127	NO	16	YES		ATD Result	
		30°	0.23	0.102	0.0329	0.053	0.188	131	NO	5	YES	200 -		
Port		40°	0.23	0.102	0.0329	0.108	0.198	156	NO	17	YES	ēj 150	156	
	Port	50°	0.23	0.102	0.0329	0.144	0.208	102	YES	10	YES	<u>E</u> 100	84 10291 74 65 55 ATT	
		60°	0.23	0.102	0.0329	0.171	0.22	91	YES	17	YES	11 ⁵⁰	16 17 17 21 38 ATMM	
		70 °	0.23	0.102	0.0329	0.193	0.232	74	YES	3	YES	0	10 20 30 40 50 60 70 80 90	
		80°	0.23	0.102	0.0329	0.212	0.246	65	YES	21	YES		Change of course (°)	
		90°	0.23	0.102	0.0329	0.230	0.263	55	YES	39	YES			

Table 2: Manoeuvring analysis result for deep water (Source: Authors)

Table 3: Manoeuvring analysis result for shallow water (Source: Authors)

Location and ENC	Side	θ	d _{adv} (nm)	d _{trs} (nm)	d _{CG} (nm))P	XTE	O < XTL	(119.8	5m) ?	Comparison Graph
number Daltimara		100	0.00	0.120	0.0000	A11	IAIF	A11	(m)	1A1	F(m)	
Baltimore		10°	0.29	0.139	0.0329	-0.498	0.196	71	YES	12	YES	XTD Result
, USA		20°	0.29	0.139	0.0329	-0.092	0.208	112	YES	4	YES	ATD Result
ENC		30°	0.29	0.139	0.0329	0.049	0.221	185	NO	3	YES	200 1 ¹⁸⁵
number:	ard	40°	0.29	0.139	0.0329	0.124	0.234	146	NO	4	YES	150 146 126
4414n120	urbo	50°	0.29	0.139	0.0329	0.173	0.249	98	YES	6	YES	\underbrace{E}_{71} 100 $\underbrace{71}_{98}$ $\underbrace{98}_{88}$ 90 $\underbrace{104}_{90}$ ATT
	Sta	60°	0.29	0.139	0.0329	0.210	0.264	88	YES	19	YES	E 50 12 4 24 40 59 ATMM
38°55.21'		70 °	0.29	0.139	0.0329	0.239	0.281	90	YES	24	YES	
N		80°	0.29	0.139	0.0329	0.265	0.301	104	YES	40	YES	Change of course (°)
076°24.7		90°	0.29	0.139	0.0329	0.290	0.323	126	NO	59	YES	
8'W -		10 °	0.28	0.132	0.0329	-0.472	0.189	64	YES	5	YES	VTD Bocult
10.7-14m		20°	0.28	0.132	0.0329	-0.092	0.201	127	NO	2	YES	ATD Result
(shallow		30°	0.28	0.132	0.0329	0.048	0.213	203	NO	1	YES	250
water)		40°	0.28	0.132	0.0329	0.120	0.226	178	NO	3	YES	
	Port	50°	0.28	0.132	0.0329	0.166	0.239	137	NO	9	YES	\underbrace{E}_{100} 127 137 137 103^{120} ATT
		60°	0.28	0.132	0.0329	0.201	0.254	103	YES	15	YES	50 64 ATMM
	70 °	0.28	0.132	0.0329	0.229	0.27	120	NO	27	YES	$0 \frac{5}{2} \frac{2}{3} \frac{3}{9} \frac{9}{15} \frac{15}{10} \frac{10}{10} \frac{20}{10} \frac{30}{10} \frac{40}{50} \frac{50}{60} \frac{60}{70} \frac{80}{80} \frac{90}{90} \frac{10}{10} \frac{10}{1$	
		80°	0.28	0.132	0.0329	0.254	0.289	143	NO	40	YES	Change of course (°)
		90°	0.28	0.132	0.0329	0.277	0.31	158	NO	52	YES	

4.3 FIRST PHASE ANALYSIS – XTL COMPLIANCE

4.3.1 10° and 20° change of course negative value

The estimated dWOP value for all conditions analyses using the ATT method was negative at 10° and 20° turns, meaning the turn had to be performed beyond the WPT, which was contradictory as the ship is already overshoot. As a result, negative value dWOP was executed exactly at WPT.

4.3.2 Compliances with XTL

In the deep water region, a bulk carrier in ballast condition was used for the first simulation analysis. Just half of the turns were compatible with XTL when using ATT. When the ship used the IATF, however, its XTL adherence improved to 100%.

The same bulk carrier at ballast was used in the second simulation analysis in a shallow water. When the simulation carried out by referring to the WOP calculated using ATT, results show only 50% of the XTD complied to XTL. However, when the simulations changed to WOP calculated using IATF, 100% compliance was recorded.

4.4 SECOND PHASE ANALYSIS - PERCENTAGE CHANGE

Classes		Water		XTI	D (m)	% Change	% Change of XTD	
course	Condition	depth	Direction	ATT	IATF	Individual turn	Average	
		Doon	Starboard	58	20	-65.5%		
100	Dallast	Deep	Port	84	6	-92.9%	-83.4%	
10°	Banast	Shallow	Starboard	71	12	-83.1%		
		Shahow	Port	64	5	-92.2%		
		Doon	Starboard	115	25	-78.3%		
200	Dollast	Deep	Port	127	16	-87.4%	-90.1%	
201	Danast	Shallow	Starboard	112	4	-96.4%		
		Shallow	Port	127	2	-98.4%		
	Ballast	Doon	Starboard	119	8	-93.3%	-96.9%	
200		Deep	Port	131	5	-96.2%		
50*		Shallow	Starboard	185	3	-98.4%		
			Port	203	1	-99.5%		
	Ballast	Doon	Starboard	125	30	-76.0%	-90.2%	
100		Deep	Port	156	17	-89.1%		
401		Challery	Starboard	146	4	-97.3%		
		Shallow	Port	178	3	-98.3%		
		Deen	Starboard	105	2	-98.1%	-93.9%	
509	D 11 (Deep	Port	102	10	-90.2%		
50*	Danast	01 11	Starboard	98	6	-93.9%		
		Shallow	Port	137	9	-93.4%		
60°		Deen	Starboard	83	12	-85.5%		
	Ballast	Deep	Port	91	17	-81.3%	82 70/	
		Ch all arr	Starboard	88	19	-78.4%	-82.1%	
		Shahow	Port	103	15	-85.4%		
	Ballast	Deep	Starboard	50	2	-96.0%	-85.7%	

Table 4: Percentage change of XTD by change of course (Source: Authors)

70°			Port	74	3	-95.9%		
		Challery	Starboard	90	24	-73.3%		
		Shahow	Port	120	27	-77.5%		
80°		Doon	Starboard	48	19	-60.4%		
	Ballast	Deep	Port	65	21	-67.7%	-65.4%	
		Shallow	Starboard	104	40	-61.5%		
		Shahow	Port	143	40	-72.0%		
90°	Ballast	Doon	Starboard	45	22	-51.1%		
		Deep	Port	55	39	-29.1%	-50.1%	
		C1 11	Starboard	126	59	-53.2%		
		Snallow		Port	158	52	-67.1%	

The negative percentage change specified the reduction of XTD by per cent. As a result, during the manoeuvring analysis, a considerable reduction in XTD was observed. It can be seen from table 4, that during manoeuvring analysis in deep water, the XTD was reduced by 51.1% - 98.1% for starboard alteration, while for manoeuvring analysis with port alteration, the XTD was successfully reduced by 29.1% - 95.9%. Meanwhile, in shallow water, XTD for starboard manoeuvring analysis was reduced by 53.2% - 98.4%, and reduction by 67.1% - 99.5% for port manoeuvring analysis. Average XTD reduction for all analysis ranged from 50.1% to 96.9%.

When this study changed from ATT to IATF during the manoeuvring analysis, the results showed the XTD was reduced significantly. The series of reduction for every 10° course alterations indicated the ship was manoeuvring closer to the course line.

5.0 CONCLUSION

Ships navigate from one destination to the next by following the course line plotted out by the navigation officer. Staying on the intended course line is critical for the ship's safety and will help reduce fuel consumption. However, most importantly, it will keep the vessel safe, as many incidents have occurred due to not staying on the charted course. Therefore, this study aims to examine the ATT and determine how it could be improved so that an accurate WOP can be calculated to reduce XTD while turning.

This study discovered that the ATT, one of the methods of assessing WOP, can be improved after an initial practical exercise using a ship simulator. By understanding the research gap IATF was successfully developed. To verify the effectiveness of IATF compared to ATT, the study calculated WOP for a set of charted courses and executed the manoeuvring analysis using the Wartsila ship simulator. It can be concluded that this study has achieved its objective by improving the method of calculating WOP. WOP can also be utilised as an abort point where it indicates the final point to alter course, or else the ship will overshoot.

5.1 RESEARCH CONTRIBUTION

The IATF may be utilized as an algorithm in the ECDIS to improve a ship's safety since it was created to considerably lower the XTD and is ideal for usage onboard merchant ships as one of the ways for estimating WOP, particularly while turning in a restricted water or during pilotage. During route planning, an ECDIS equipped with pre-installed vessel manoeuvring data may automatically calculate the WOP for each course change based on the vessel's state, such as ballast and loaded condition. As a consequence of this research, IATF integrated with the ECDIS may identify when the navigator performs an inaccurate WOP calculation, and the

ECDIS may provide a warning showing the wrong input. As a result, this issue may be resolved utilising the integrated IATF.

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